

Introduction to Optics part II

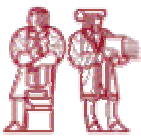
Overview Lecture

Space Systems Engineering

presented by: [Prof. David Miller](#)

prepared by: Olivier de Weck

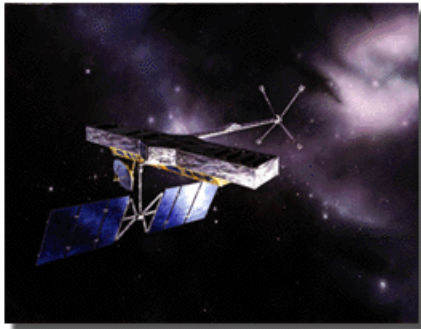
Revised and augmented by: Soon-Jo Chung



Interferometer Types (NASA, AirForce)

SIM-2006

Michelson Interferometer
Precision Astrometry



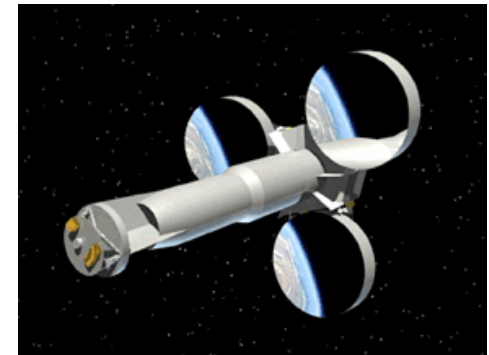
Space Technology 3-2005

Michelson Interferometer



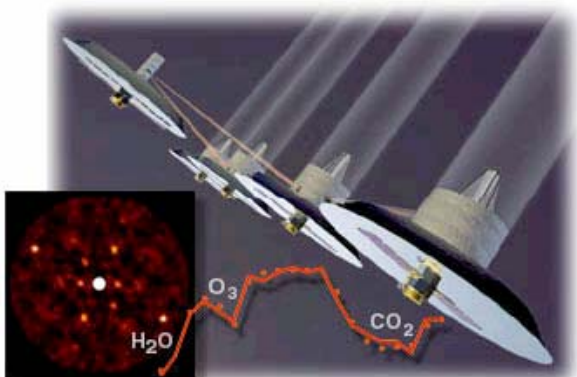
Air Force UltraLITE

Fizeau Interferometer
Earth Observing Telescope



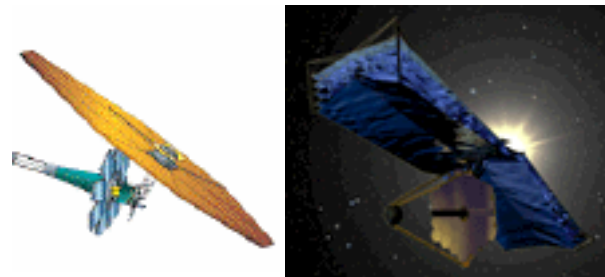
TPF - 2011

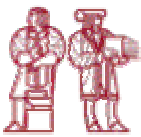
Michelson Interferometer



NGST - 2007

A Common Secondary Mirror (MMT, Fizeau)
Primary Mirror = 8 m diameter





Interferometer Types (Ground)



Keck Interferometer-2006

Michelson Interferometer (Infrared)

Twin 10 m Keck Telescopes and four 1.8 m outriggers
Baseline 85m



Palomar Testbed Interferometer

Michelson Interferometer (Infrared)

Testbed for Keck and SIM

Mark III Interferometer

Michelson Interferometer (Visible)



Keck Observatory:

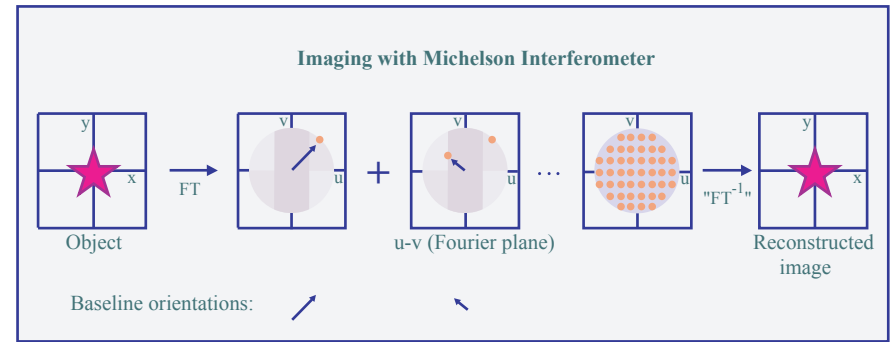
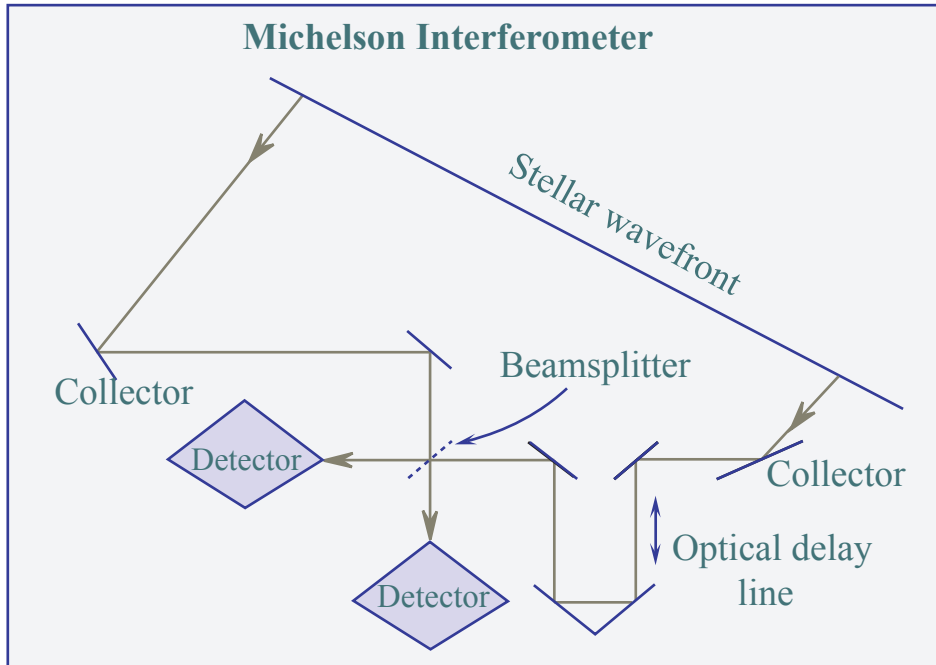
Multiple Mirror Telescope (MMT)

Fizeau Interferometer (Visible, Infrared)

36 hexagonal segments => 10 m overall aperture



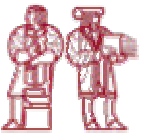
Michelson Interferometer



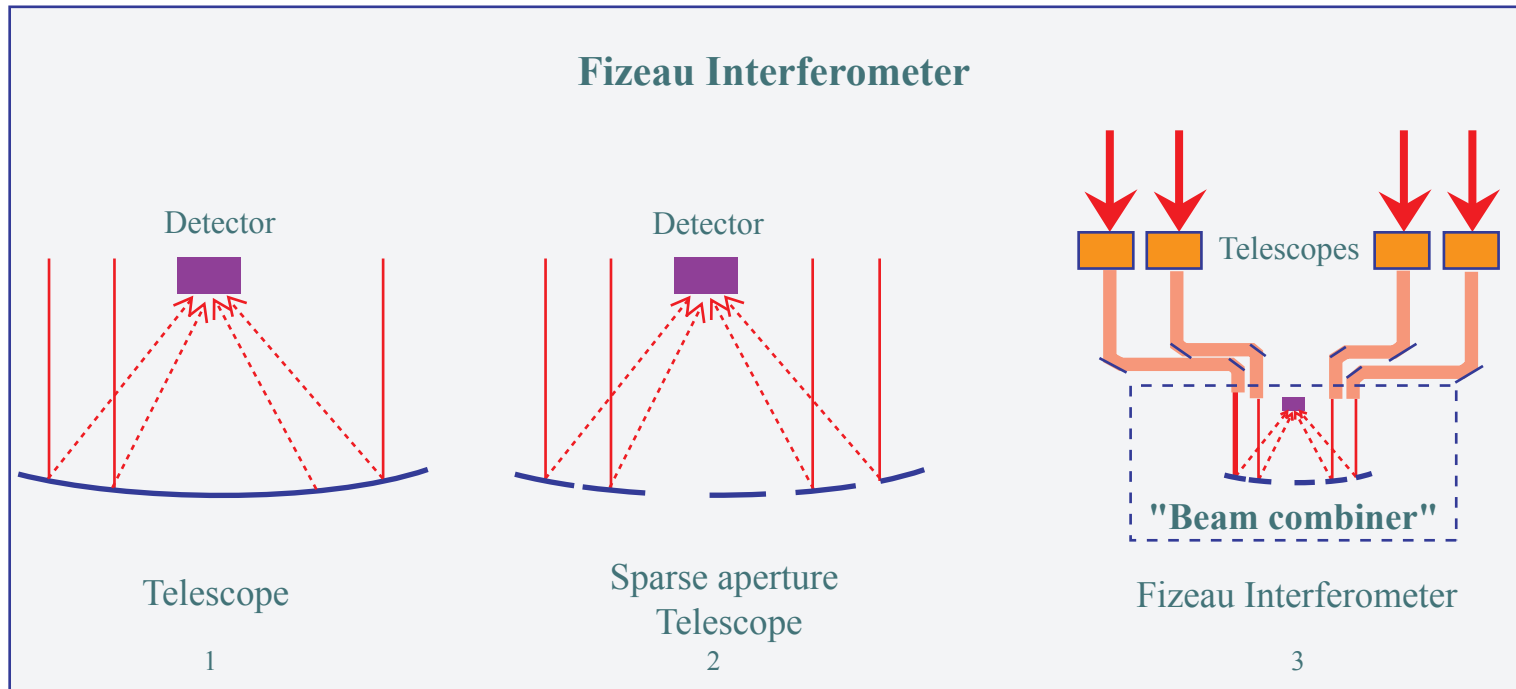
Independent Light Collectors feed light to a common beam combiner. Get interfered fringes => Inverse Fourier Transform (CLEAN, MEM)



**Suitable for Astronomical Objects:
Unchanged over a long period of time**



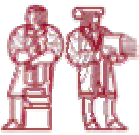
Fizeau Interferometer



Gives a direct image of a target from a large combined primary mirror, and a wide field of view (Imaging applications in space and MMT)

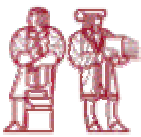


**Suitable for Wide Angle Astrometry
And for rapidly changing targets (Terrestrial, Earth Objects)**

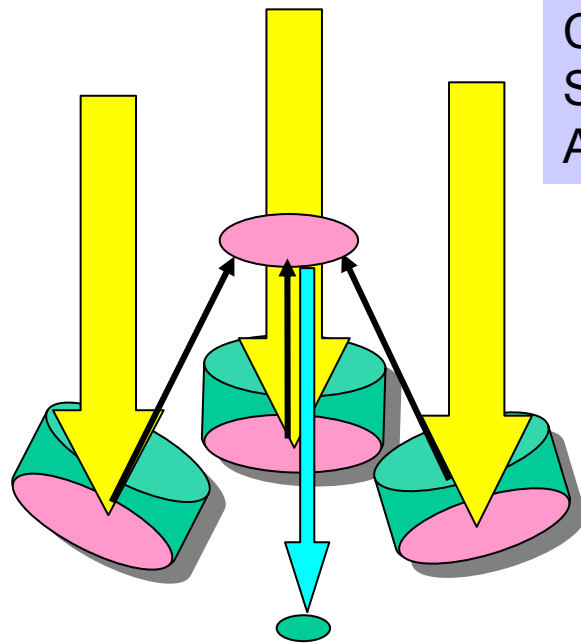


Comparison (Fizeau, Michelson)

<i>Fizeau Interferometer</i>	<i>Michelson Interferometer</i>
Produce a direct image of its target (Full Instant u-v coverage provided)	Takes a subset of u-v points obtained a period of time.
Wide angle(field) of view imaging applications	Astronomy, Nulling Interferometry
Rapidly Changing targets (Terrestrial, Earth Objects)	Target unchanged (Astronomical Objects)
Takes the combined science light from all the apertures and focuses it into CCD	Measures points in Fourier transform of images => Inverse FFT needed
U-V resolution depends on both the separation and the size of apertures	Angular resolution depends solely on the separation of apertures
Optimal Configuration: Golay (minimum aperture size)	The angular resolution improves as the separation increases

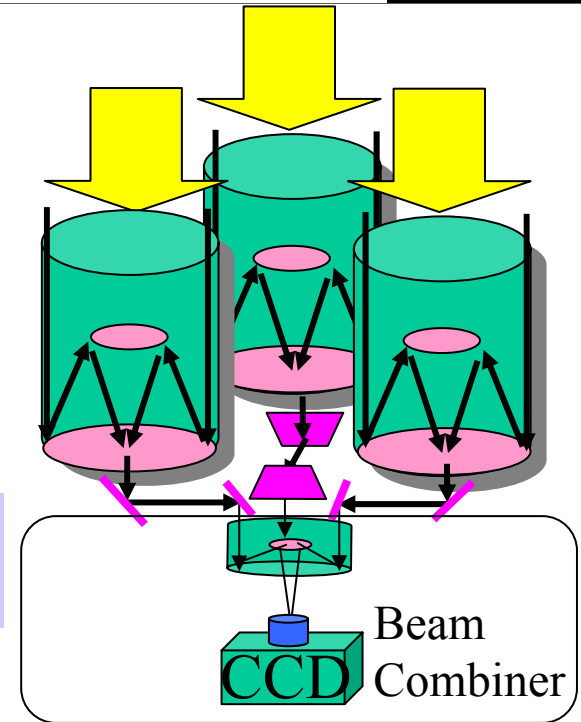


Common Secondary vs Sub Telescope



Common Secondary Mirror Array

Phased Sub-Telescope Arrays



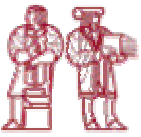
Common Primary

Precise Off Axis Configuration
 Off Axis Optical Aberration
 Less Central Obstruction(Off Axis)
 Hard to change the Configuration

Sub Telescope Fizeau

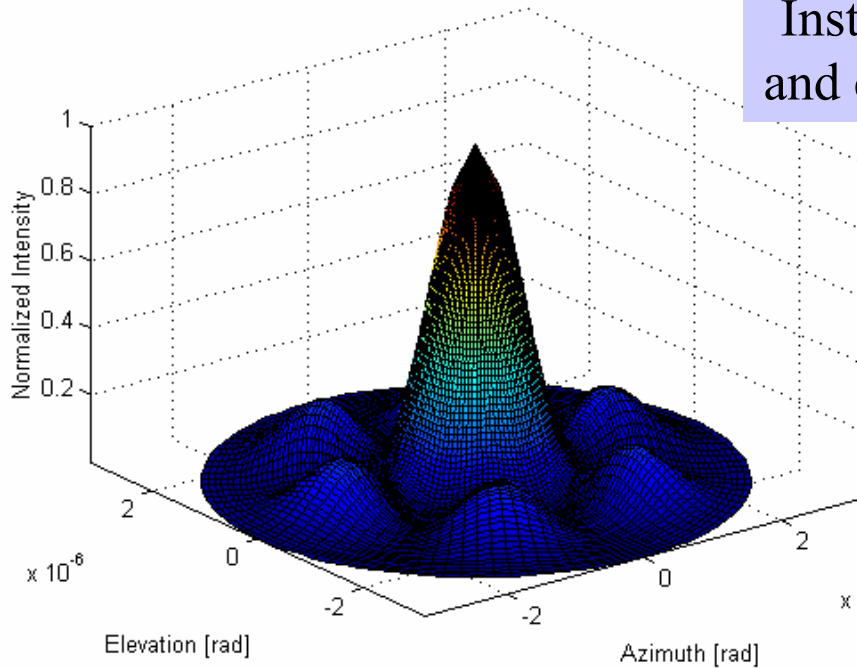
Need Combiner + Phase sensing and compensater mechanism (complex)
 On Axis Suffers Central Obstruction
 Can employ Off-the-shelf telescopes

AirForce is studying two options for UltraLITE(Golay 6)



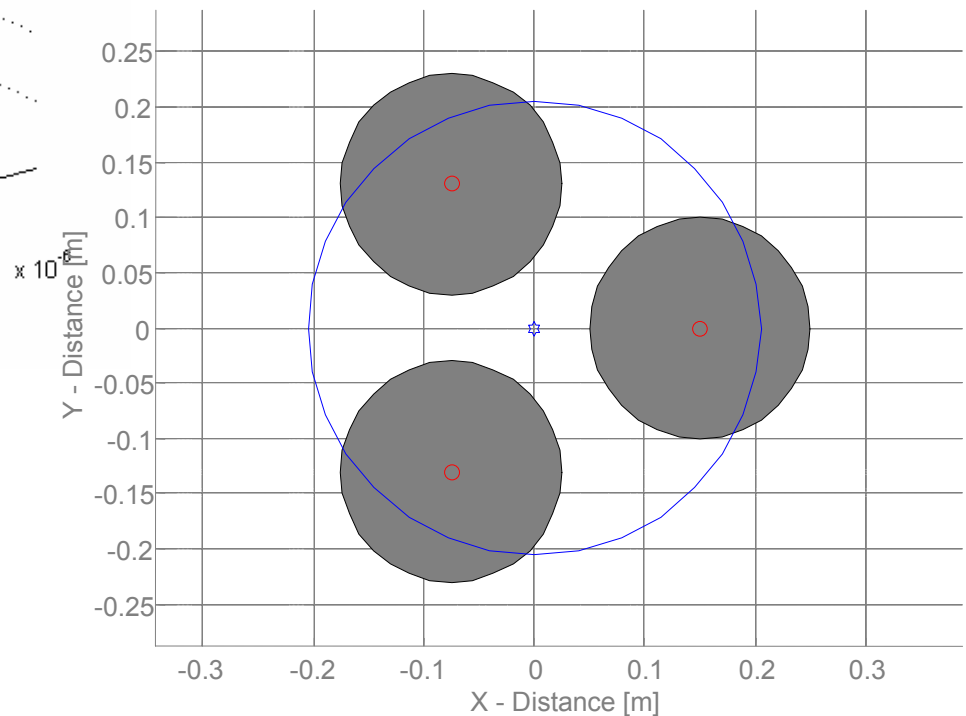
Optical Arrays

Instead of using a single aperture use several and combine their light to form a single image



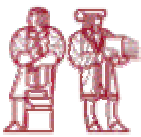
Aperture positions (uv) are critical - look at combined PSF / Transmissivity of the Optical Array

Optical Array Configuration

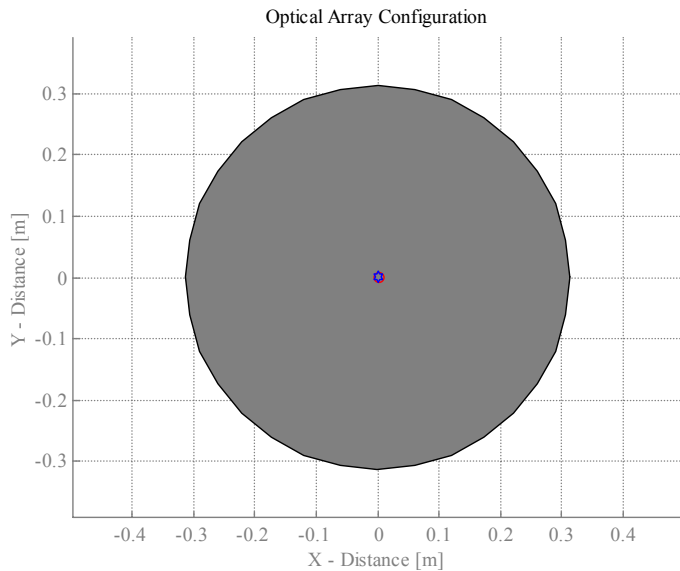


Transmissivity Function:

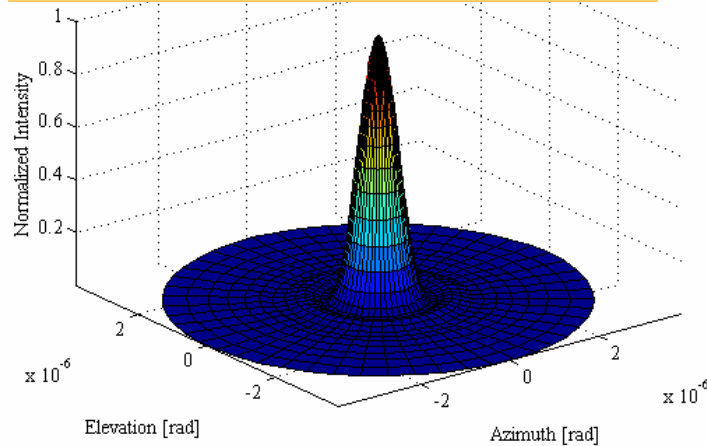
Derivation see separate
handout (Mennesson)



CDIO: Breaking the Paradigm



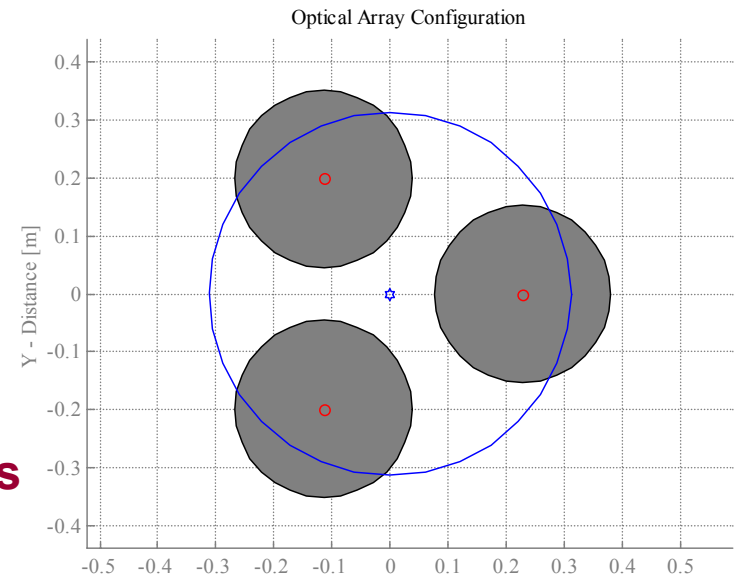
Monolithic 0.6 m telescope



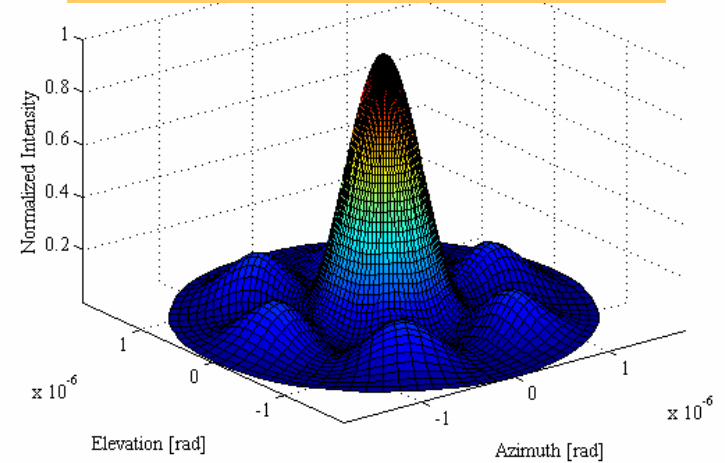
Physical Aperture Layout

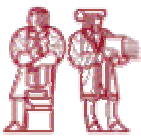
Compare Architectures with Quantitative Metrics

PSF

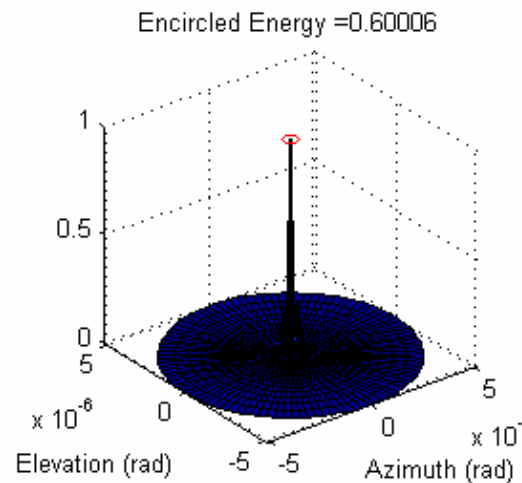
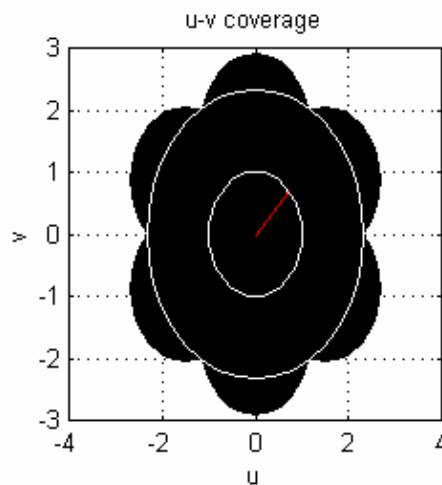
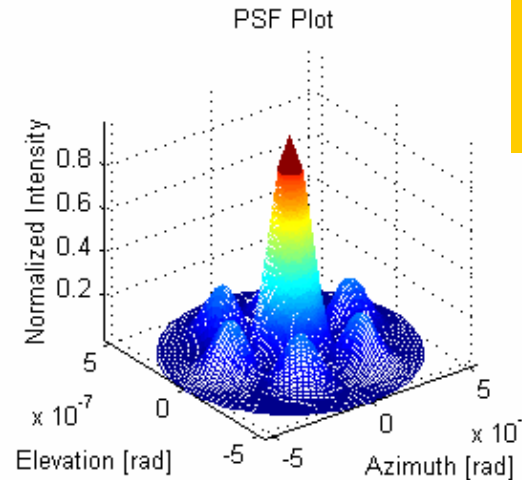
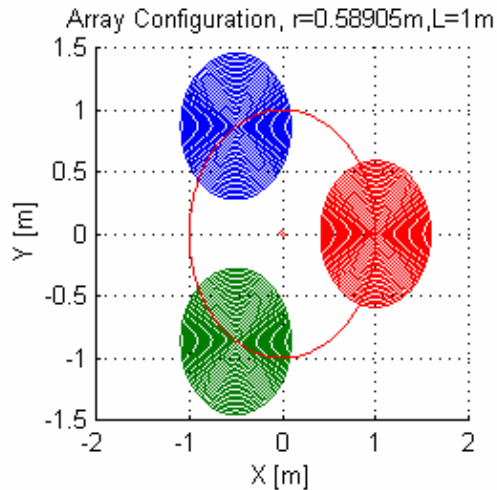


Golay-3 0.6 m telescope





Effective Radius of Optical Array



How to find the effective radius (R_{eff}) of the array?

- R_{eff} = the radius of the array thought as that of a monolithic aperture.

- UV coverage plot

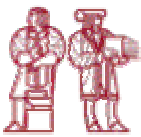
$$u = \pm \frac{x_2 - x_1}{\lambda} \quad v = \pm \frac{y_2 - y_1}{\lambda}$$

x, y is any point within aperture

- R_{uv} : the maximum radius of uv plot without any holes

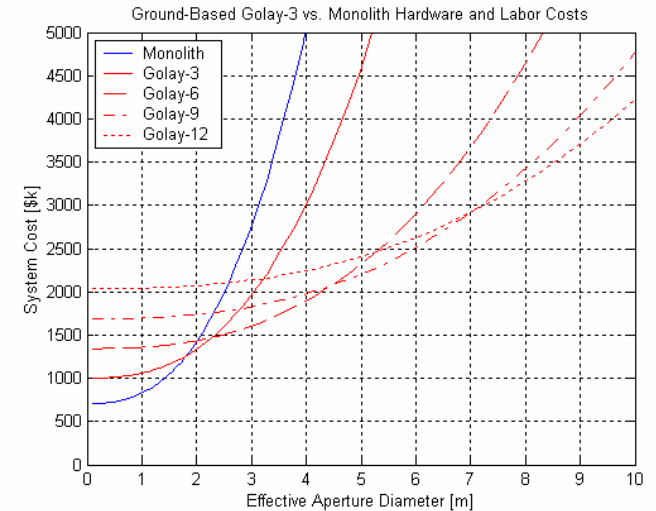
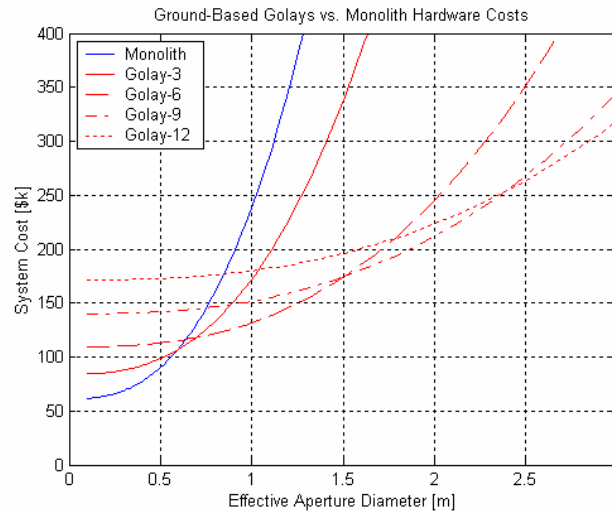
- $R_{eff} = 0.5 R_{uv}$

- Fill Factor: the array's total collecting area over the area of a filled aperture with the same uv coverage (the same R_{eff})



Golay Configurations

- Optimum Golay is D_{eff} -dependent
- Labor moves Golay benefits to larger D_{eff}
- Golay's sacrifice Encircled Energy



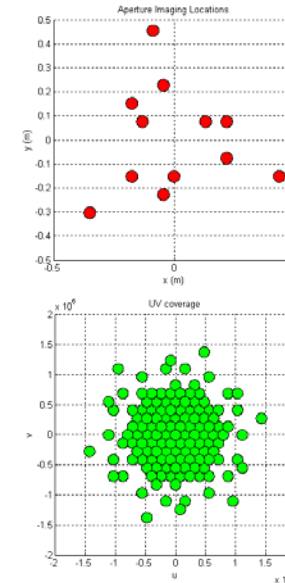
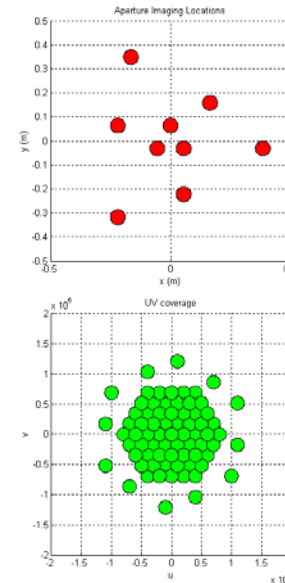
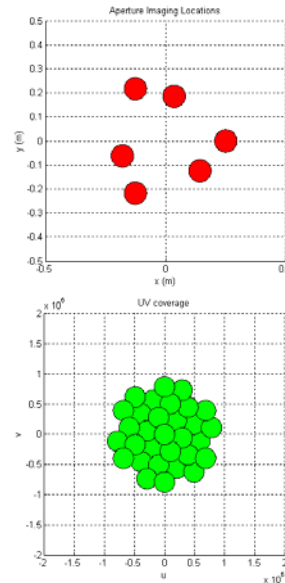
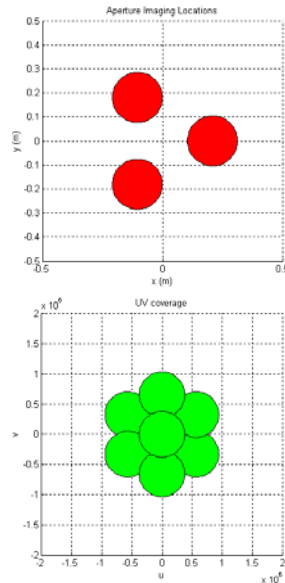
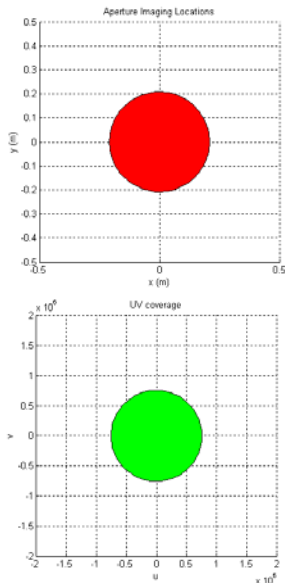
EE=83.5%

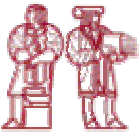
EE=26.4%

EE=9.3%

EE=3.6%

EE=2.2%





Technological Trends

- Lightweight (Low-Area-Density) Optics - 15kg/m^2
- Deployable Optics
- Adaptive and Active Optics
- Membrane Mirrors and Inflatables
- Ultra-Large Arrays (CCD Mosaics)
- Distributed Optical Arrays
- Space Based Astronomy
- White light interferometry



Optical Performance Criteria

- **Sensitivity(Effective Collecting Area)**
- **Point Spread Function(PSF):** Frequency used merit function(Irradiance distribution), Can measure Phase difference, can derive Resolution, EE, MTF(OTF)
- **Encircled Energy:** particularly relevant merit function of the optic performance of an optical system whose purpose is to collect light and direct it thru the entrance slit of a spectrometer
- **Modulation Transfer Function(MTF):** For many imaging applications involving extended objects containing fine structure, the MTF is a more appropriate performance criterion than PSF. Practical Cutoff Frequency(F_r) -> Cutoff Frequency(F_c)



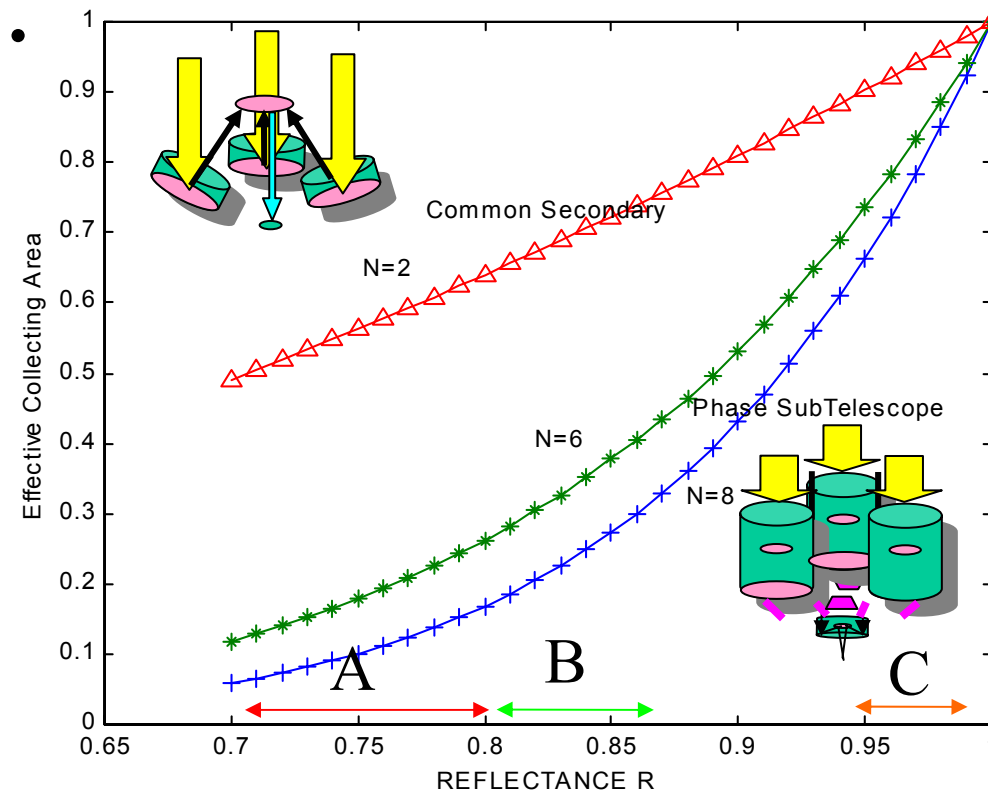
Optical Sensitivity

- Sensitivity of Phased Telescope Array (Effective Collecting Area)

R: the reflectance

N: the number of reflections

$$A_{eff} = A_{geo} R^N$$

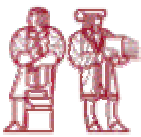


2 types may be viable concept for quasi-monochromatic applications; however, phased telescope arrays will suffer substantial sensitivity losses for broadband spectral applications

A Region: UV

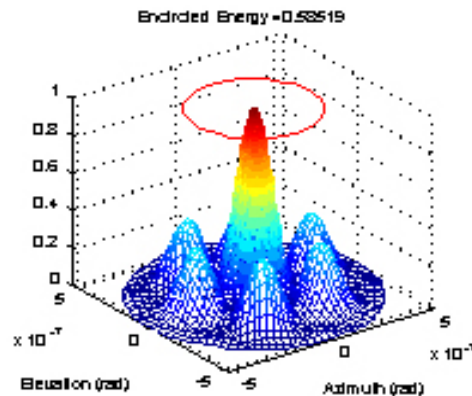
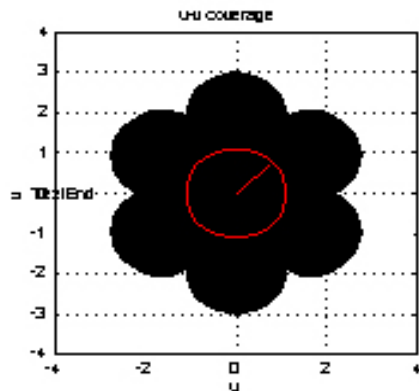
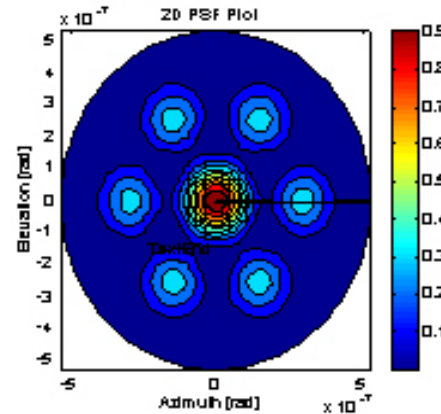
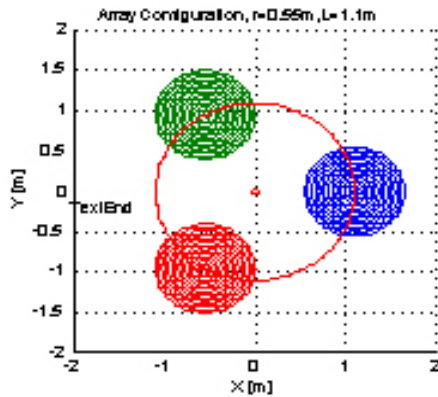
B Region: Visible (Color)

C Region: Quasi-Monochromatic



PSF,EE (Golay Array –3)

Preliminary Calculation(0.3m GR) => D=2.0m,approx needed !!
For $R_{eff}=1m$, $r=0.5m$ and Array Radius(L)= 1.m (Golay 3,monochrome)
 $r=0.3685m$ and Array Radius(L)= 1.1m (Golay 6,monochrome)



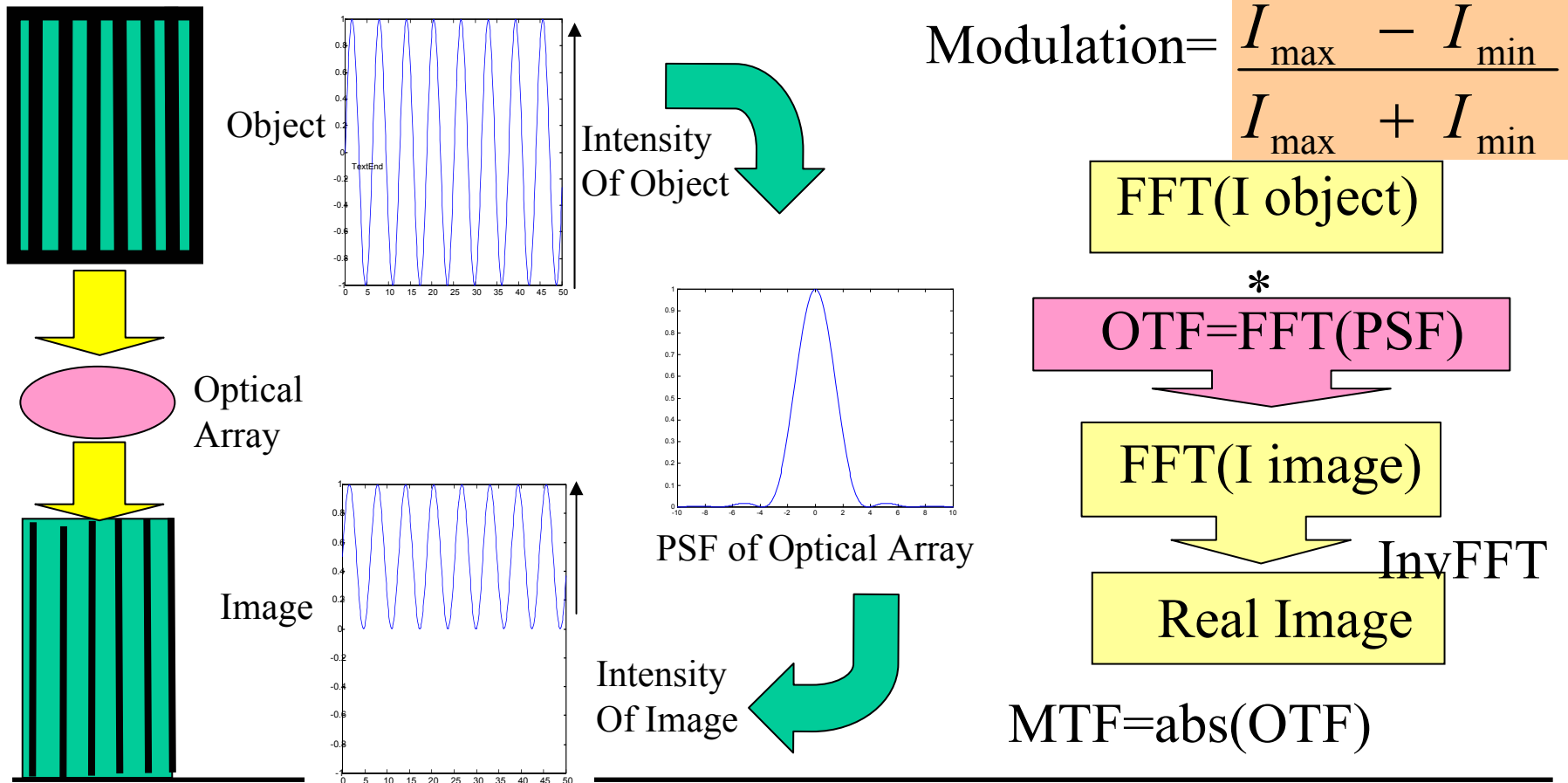
Using Analysis
Tool:
Evaluate
Configuration
Using

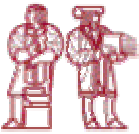
- PSF(Point Spread Function)
- Encircled Energy
- MTF(Modulation Transfer Function)
- FF(Fill Factor)



Modulation Transfer Function

- An image of an extended object is far more complex than point source (e.g. astrometry). PSF is not enough! -> MTF of each configuration is necessary
- Both Resolution and Contrast (Modulation) Transfer IMPORTANT





Optical Control and Beam Combining

Optics Control

Actuators

Piezoelectric translators (PZTs)

Fast steering mirrors (Tilt and Tip)

Optical delay lines (or inchworm positioners)

Alignment mirrors

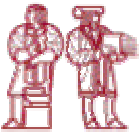
Sensors

Laser interferometers

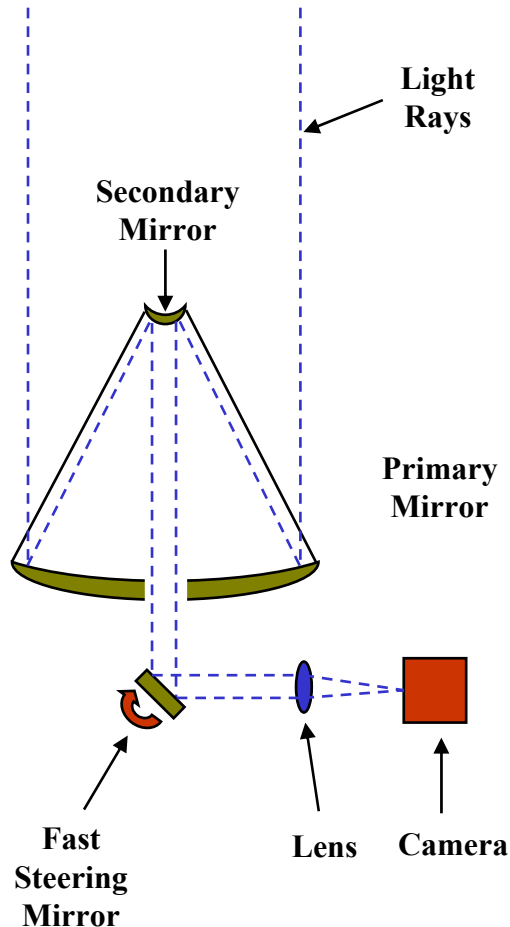
Quad cells

Charge Coupled Device (CCDs) cameras

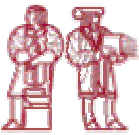
Avalanche Photo Diodes (APDs)



Fine Optical Pointing and Phasing: Single Aperture



- Light path
 - Light enters spacecraft by reflecting off primary and then secondary, after which it is collimated (not converging or diverging except for diffraction effects)
 - Reflects off two-axis (tip and tilt) Fast Steering Mirror (FSM)
 - FSM controls out the low level line-of-sight (LOS) jitter in the deadband of the attitude control
 - Lens focuses light onto camera
- LOS jitter control using FSM
 - Feedforward attitude sensors to command FSM
 - If bright point source in FOV, measure motion on camera and command FSM to minimize its motion



Beam Combiner

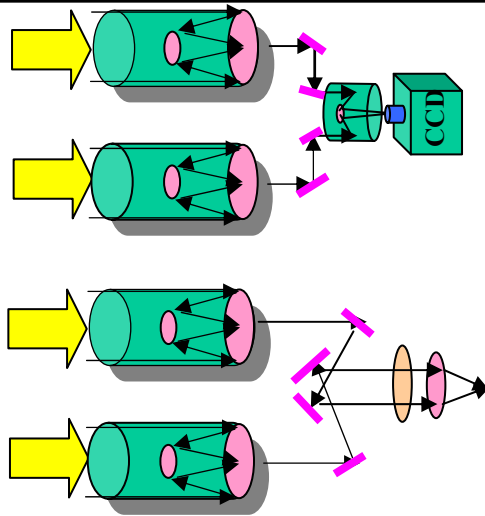


Fig.10, Cassegrain Type beam combiner (above) and refractive lens combiner

Phase(Piston Error) Contributor:

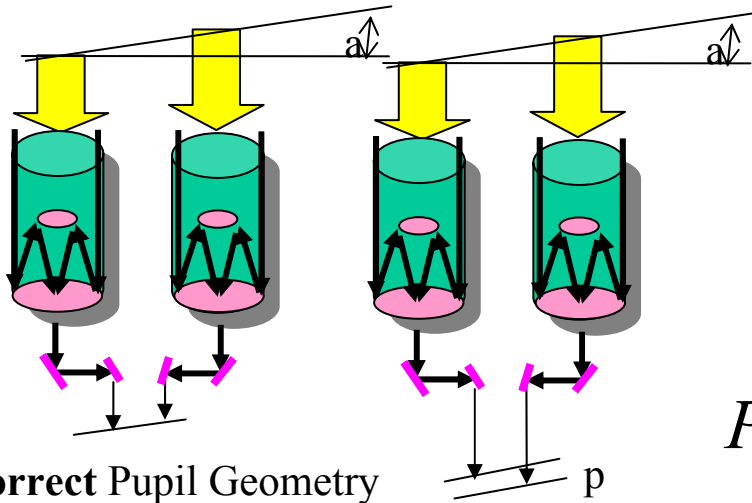
1. Lateral Pupil Geometry Error (Pupil Mapping Error)
=>the elimination of this error : golden rule of separated telescope (significant in wide field of view telescope)
2. Piston Error: part of piston error is induced by pupil geometry e
3. Tilt Error : Measured separately from piston error. X-Tilt Error, Y-Tilt Error

Beam Combining Goal:

1. maintain the optical phase difference of each beam to a fraction of a wavelength
 2. align images from telescopes to within a fraction of a resolution element over the whole field of view
- (Additionally) Field of curvatures on the order of wavelength, finer than required for conventional telescopes



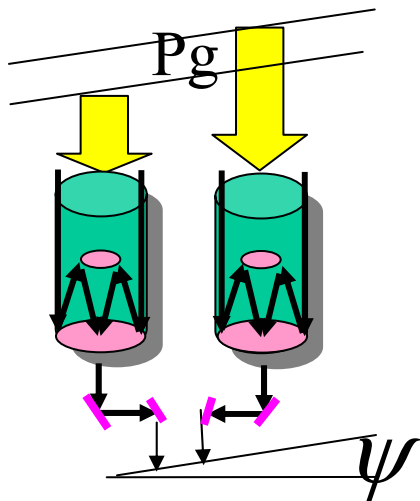
Lateral Pupil Geometry Error



Physical Meaning:
 If the subapertures of the entrance pupil have a D , and separated by S , with magnification M , the exit pupil must have dimensions for D/M and separation S/M

$$P = \varepsilon \sin(aM)$$

Incorrect Pupil Geometry



$$P_g = \varepsilon \sin\left(\frac{\psi}{M}\right)$$

ε : lateral pupil geometry error

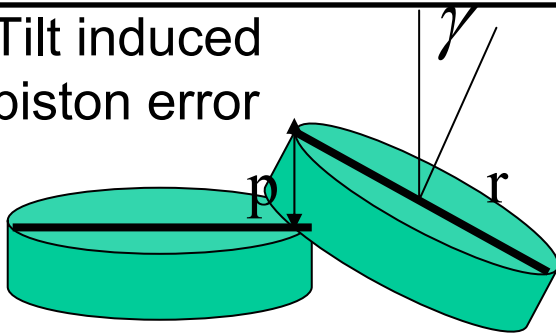
Difficult to measure lateral pupil geometry => abstract optical quantity

Use the relationship and Kalman filter to estimate ε



Optical Tolerance

Tilt induced piston error



$$P_t = r \sin(\gamma)$$

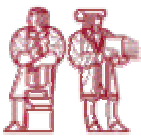
Total Piston Error

$$m_p = p_t + (p_g + p)$$

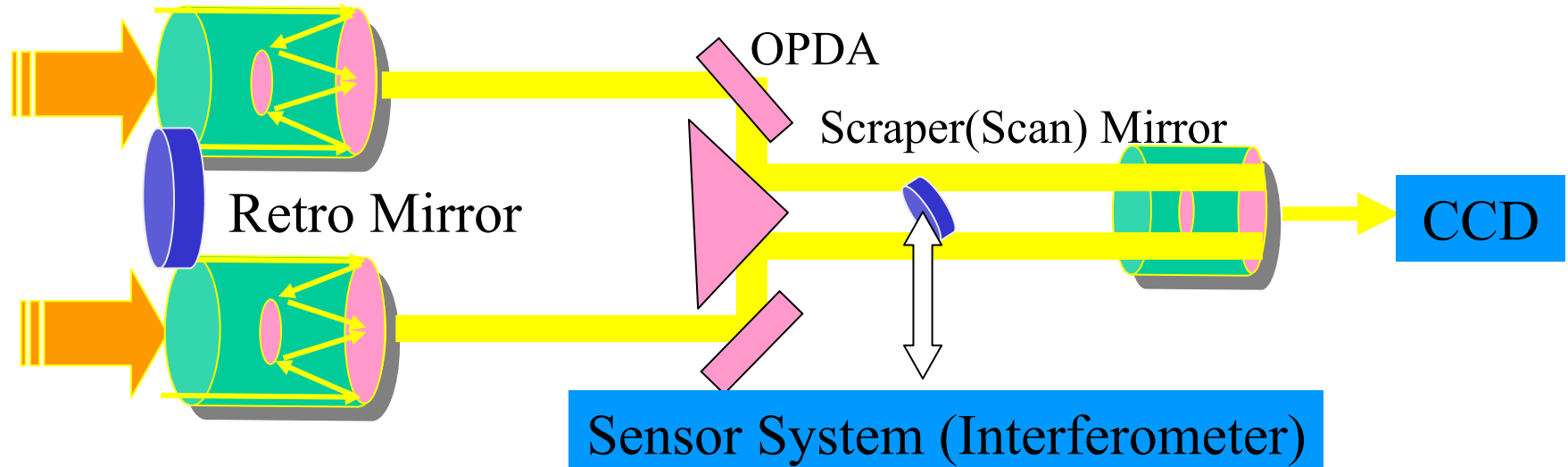
$$= r \sin(\gamma) + \left[\varepsilon \sin\left(\frac{\psi}{M}\right) + p \right]$$

P : the optical path difference between beams

Errors	Tolerance
Piston	1/10 of wavelength = 55 nm
Tilt	1/10 of λ , $r=0.5\text{m} \Rightarrow 110 \text{ nrad}$
Lateral pupil Geometry Error	FOV=4km, h=500km, piston error 55nm $\Rightarrow 1 \mu\text{m}$
Alignment Error (Image Rotation)	<1/10 of Airy Disk Diameter $\Delta\Phi < \frac{(0.1)(2.44\lambda)}{FOV_{HalfAngle} D} \mu\text{rad}$



Beam Combining Layout



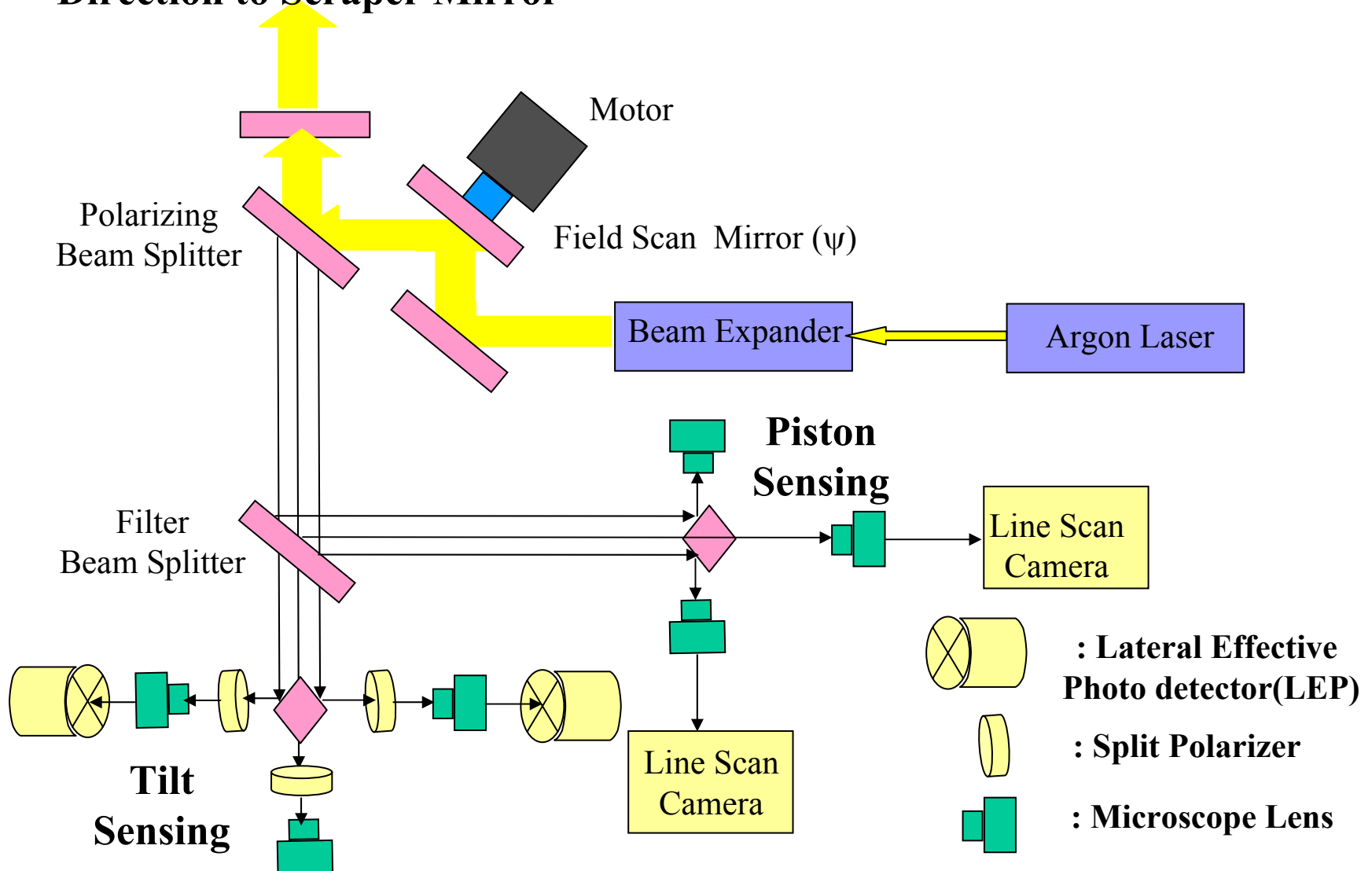
OPDA(Optical Path Difference Adjuster) :is driven by

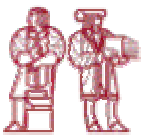
- Piezoelectric translator(PZT) = Fine Control
Translation Range ($-12 \mu\text{m}$),Resolution(5nm), SlewRate($4.5 \mu\text{m/s}$)
Angular Tilt Range($700 \mu\text{rad}$),Resolution (200 nrad)
- Burleigh inchworm positioners = Coarse Control
Translation Range(5mm) with a resolution of $0.1 \mu\text{m}$



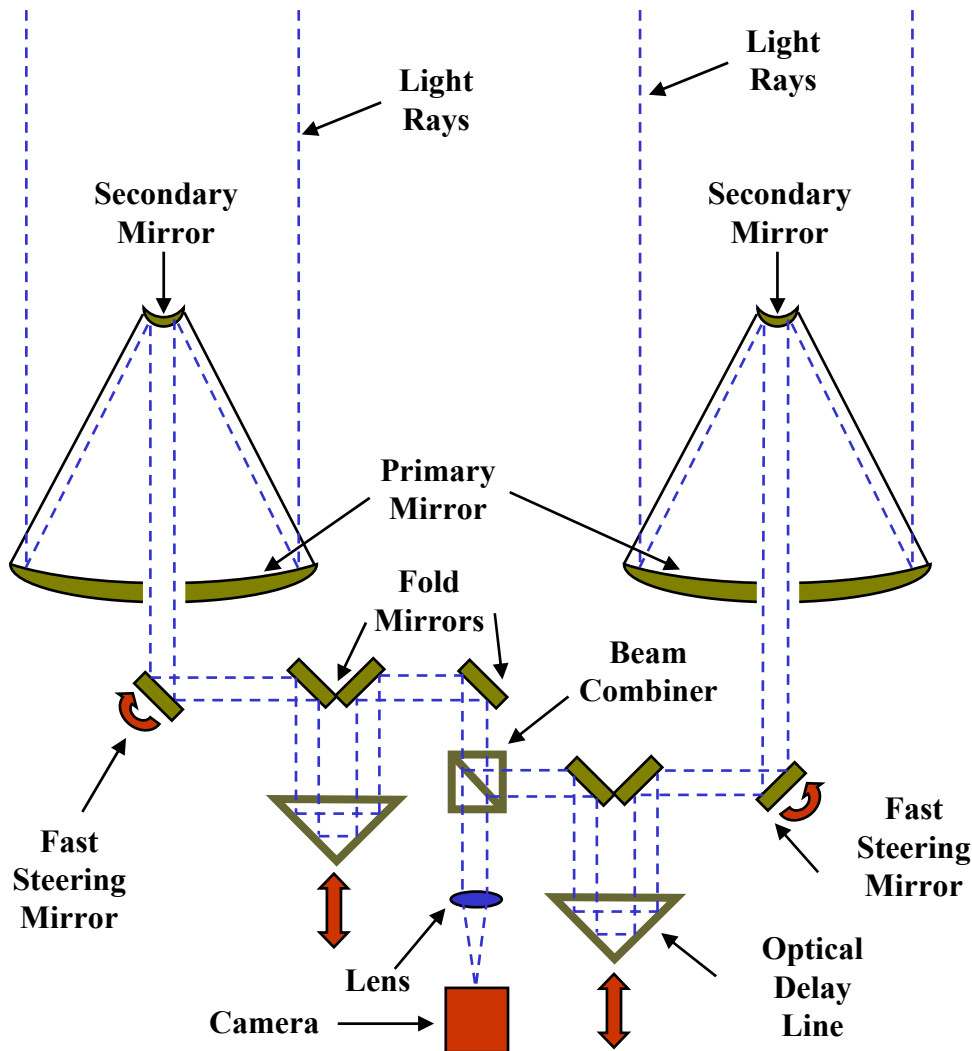
Sensor System Optics(Example from AFRL)

Direction to Scraper Mirror

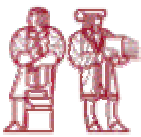




Fine Optical Pointing and Phasing: Multiple Aperture

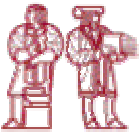


- Now need to stabilize both absolute and relative LOS jitter (Differential Wavefront Tilt)
- Also need to interfere same wavefront of light at combiner
 - Use Optical Delay Lines (ODLs)
 - ODLs add and subtract optical pathlength from the companion telescope to the combiner.
 - Used to control small positional mis-alignment and S/C attitude error
 - Typically a multi-stage device with voice coils and piezoelectrics



References

- [1] [Larson, W.J., Wertz, J.R.](#), “Space Mission Analysis and Design”, Second Edition, 9.5 Designing Visual and IR Payloads, pp.. 249-274, Microcosm, Inc,1992
- [2] [Born Max, Wolf Emil](#), “Principles of Optics”, Electromagnetic Theory of propagation interference and diffraction of light, Sixth Edition, Cambridge University Press, 1998
- [3] [Hecht E.](#) “Optics”, Addison-Wesley, 1987
- [4] [Günter Diethmar Roth](#), “Compendium of Practical Astronomy”, Volume 1, Instrumentation and Reduction Techniques, Springer Verlag, Berlin, New York, ISBN 3-540-56273-7, 1994



Optical System Design Process

From SMAD Chapter 9

1. Determine Instrument Requirements
2. Choose preliminary aperture
3. Determine target radiance
4. Select detector candidates
5. “Optical Link Budget”, SNR considerations
6. Determine Focal Plane architecture and scanning schemes
7. Select F# and telescope/optical train design
8. Complete preliminary design and check MTF
9. Estimate weight, power and ACS requirements
10. Iterate and document - code optics software module