

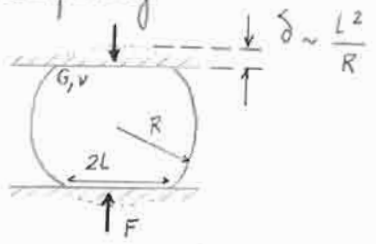
Last time:

- structural elements of the cytoplasm (cytosol, cytoskeleton)
- dimensional analysis & scaling
- cell mechanics experiments: cell indentation (elastic analysis not perfect: hysteresis)

This time:

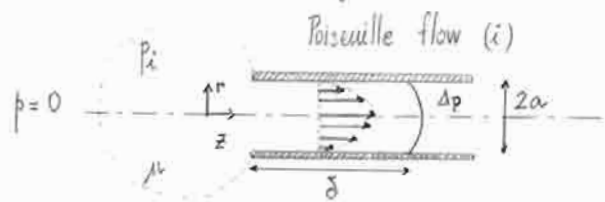
- microstructural models
- mechanotransduction
- micropipette aspiration
- microbead manipulation
- Brownian motion of microbeads

cell squashing



energy $U \sim F \delta \sim G \left(\frac{\delta}{L}\right)^2 L^3$, hence $F \sim G \delta^{1/2} R^{1/2}$

micropipette aspiration (dynamic case: $\Delta p > \Delta p_c$ critical pressure)



- assumptions:
- neglect surface tension N $p_i = 0$
 - neglect shear or bending effects in membrane
 - treat interior of cell as viscous fluid
 - neglect inertia

- Two scenarios:
- (i) no-slip boundary condition at pipette wall: $v_z(r=a) = 0$
 - (ii) membrane slides without friction inside pipette: $v_z = \frac{d\delta}{dt} = \text{uniform}$

(i) no-slip model (viscous drop)

$\Delta p \leftrightarrow \frac{d\delta}{dt}$ or $\delta(t)$?

$\nabla p = \mu \nabla^2 v_z$ } pressure ~ shear

$\frac{\partial p}{\partial z} \sim \frac{\mu}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_z}{\partial r} \right) \sim \frac{\mu}{a^2} \frac{d\delta}{dt}$ (radial gradient dominates)

$\frac{\Delta p a^2}{\mu} dt \sim \delta d\delta$ yields the relation $\delta \sim \sqrt{\frac{\Delta p a^2 t}{\mu}}$

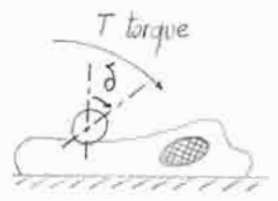
(ii) no-friction model

$\frac{\partial p}{\partial z} \sim \frac{\Delta p}{a} \sim \mu \frac{\partial^2 v_z}{\partial z^2} \sim \frac{\mu}{a^2} \frac{d\delta}{dt}$ (axial gradient at the entrance of the pipette)

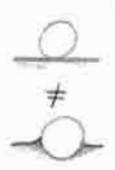
$\frac{\Delta p a}{\mu} dt \sim d\delta$ yields the relation $\delta \sim \frac{\Delta p a t}{\mu}$

(thin lubricating layer)
Dembo et al.

microbead manipulation: magnetic twisting cytometry



relationship between T and δ ? for homogeneous elastic continuum
get $G^* = G' + iG''$ (soft glassy material = cell, Fabry et al.)



• Laser tracking microrheometry (Brownian motion of beads)

access to G' and G'' (homogeneous medium)
through mean square displacement
viscous for short time, elastic for long time



□ Cell models

- viscoelastic membrane on top of viscoelastic core (bending, surface tension, elasticity scales)
Turner & Sens
not necessarily linear dependence between force (indentation) and deformation
- cellular solids model

Gibson & Ashby, 1988; Satcher & Dewey 1997
characteristic unit cell  bending of network



- tensegrity model

Donald Ingber  compressive elements
tensile elements



- biopolymer model : $k_B T$ dependence