

Homework 8

1. a. select 1.5 m as generally applicable optimal depth.
- b. For temperate climate, use areal loading rate of 80 Kg BOD/ha·day

$$\begin{aligned}\text{Daily loading} &= QC_{in} = 3800 \text{ m}^3/\text{d} \cdot 200 \text{ mg/L} \\ &\quad \cdot 1000 \text{ L/m}^3 \cdot 10^{-6} \text{ Kg/mg} \\ &= 760 \text{ Kg/day}\end{aligned}$$

$$\therefore \text{Pond size} = 10 \text{ ha} = 10^5 \text{ m}^2$$

$$\begin{aligned}\text{c. Volume} &= 1.5 \text{ m} \cdot 10^5 \text{ m}^2 = 1.5 \times 10^5 \text{ m}^3 \\ t_R &= \frac{V}{Q} = \frac{1.5 \times 10^5 \text{ m}^3}{3.8 \times 10^3 \text{ m}^3/\text{d}} = 40 \text{ days}\end{aligned}$$

$$\begin{aligned}\text{d. Volumetric load} &= \frac{760 \text{ Kg/day}}{1.5 \times 10^5 \text{ m}^3} \\ &= 5 \text{ Kg BODS}/(1000 \text{ m}^3 \cdot \text{day})\end{aligned}$$

- e. Assuming fully mixed conditions,

$$\frac{S}{S_{in}} = \frac{1}{1 + t_R K}$$

$$\begin{aligned}S &= \frac{200 \text{ mg/L}}{1 + 40 \text{ days} \cdot 0.2 \text{ day}^{-1}} \\ &= 22 \text{ mg/L}\end{aligned}$$

2.

$$Q = 4500 \text{ m}^3/\text{d}$$

$$S_{in} = 150 \text{ mg COD/L}$$

$$S = 7 \text{ mg COD/L}$$

$$\text{SRT} = \theta_c = 10 \text{ days}$$

$$\text{MLVSS} = X = 1400 \text{ mg VSS/L}$$

$$Y = 0.6 \text{ mg VSS/mg COD}$$

$$K_e = 0.06 \text{ day}^{-1}$$

From Lecture 19, Eq. 32

$$\frac{1}{\theta_c} = YU - K_e = \frac{1}{10 \text{ d}} = 0.6 U - 0.06 \text{ d}^{-1}$$

$$U = (0.1 + 0.06) \text{ d}^{-1} / 0.6 \frac{\text{mg VSS}}{\text{mg COD}} = 0.27 \frac{\text{g COD}}{\text{g VSS} \cdot \text{d}}$$

From Lecture 19, Eq 26

$$\begin{aligned} U &= \frac{S_{in} - S}{t_R X} = \frac{(150 - 7) \text{ mg COD/L}}{t_R \cdot 1400 \text{ mg VSS/L}} \\ &= 0.27 \frac{\text{mg COD}}{\text{mg VSS} \cdot \text{d}} \end{aligned}$$

$$t_R = \frac{143}{0.27 \cdot 1400} = 0.38 \text{ day} = 9 \text{ hours}$$

$$V = t_R Q = 1700 \text{ m}^3$$

$$\begin{aligned} \text{b. } \frac{F}{M} &= \frac{S_{in}}{t_R X} = \frac{150 \text{ mg COD/L}}{1400 \text{ mg VSS/L} \cdot 0.38 \text{ d}} \\ &= 0.28 \frac{\text{kg COD}}{\text{kg VSS} \cdot \text{d}} \end{aligned}$$

c. From Lecture 19, Equation 12

$$\begin{aligned}
 P &= \frac{QY(S_{in}-S)}{1 + \theta_c k_c} \\
 &= \frac{4500 \frac{m^3}{d} \cdot 0.6 \frac{mg \text{ VSS}}{mg \text{ COD}} \cdot (150-7) \frac{mg \text{ COD}}{L} \cdot 10^3 \frac{L}{m^3} \cdot \frac{Kg}{10^6 mg}}{1 + 10 d \cdot 0.06 d^{-1}} \\
 &= 241 \text{ Kg VSS/d}
 \end{aligned}$$

$$\begin{aligned}
 d. \quad X_r &= \frac{1}{SVI} = \frac{1}{100 \text{ mL/g}} \\
 &= 0.01 \frac{g}{mL} = 10,000 \frac{mg}{L}
 \end{aligned}$$

From Lecture 19, Eq. 37

$$\begin{aligned}
 \theta_c &= \frac{t_R}{1+r-r(X_r/X)} \\
 10 d &= \frac{0.38 d}{1+r-r(10000/1400)} \rightarrow r = 0.16
 \end{aligned}$$

e. From Lecture 20, pg 11

$$\begin{aligned}
 R_{O_2} &= Q(S_{in}-S) - 1.42 P \\
 &= 4500 \frac{m^3}{d} (150-7) \frac{mg \text{ COD}}{L} \cdot 10^3 \frac{L}{m^3} \cdot \frac{Kg}{10^6 mg} \\
 &\quad - 1.42 \frac{Kg \text{ COD}}{Kg \text{ VSS}} \cdot 241 \frac{Kg \text{ VSS}}{d} \\
 &= 300 \text{ Kg COD/d} = 300 \text{ Kg O}_2/\text{d}
 \end{aligned}$$